Testing Hypotheses

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The role of Hypotheses in the Scientific Method



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The role of Hypotheses in Quantitative Studies

testable by considering the observed data as values taken from a collection of random variables.

The difference between the two models (the actual and random one) is actual data is unlikely to have occurred randomly.

If we can reject (through testing) the null hypothesis, we have ground for believing that there is a (dependence) relationship between two or more hypotheses) is called **alternative**.

- In quantitative studies, hypotheses are **statistical hypotheses**, i.e., they are
- deemed statistically significant if, according to a threshold probability, the
- The hypothesis that the two models are comparable is called **null hypothesis**.
- phenomena represented by the data. This second hypothesis (or class of



Towards testing for correlation in network studies

The term "correlation" refers to the degree to which a pair of variables are linearly related. Correlations are useful because they can indicate a predictive relationship — not necessarily a causal one.

To test the hypothesis of correlation, we measure a set of variables (e.g., two) on a set of cases drawn via a probability sample from a population and then calculate a correlation coefficient between the variables.

If the correlation measure found in the sample appears in rare cases with respect to all possible random configurations - usual measures are 5%, 1% or 0,1% - we have a high degree of confidence in rejecting the null hypothesis (that the two variables are independent) and accept the alternative (that they are correlated).

The most common of correlation coefficients is **Pearson's coefficient**.



Testing Hypotheses in Network Analysis

Applying correlation tests over <u>network data has some peculiarities</u>, mainly because standard (statistical) tests make assumptions about the data which are violated by network data.

E.g., standard tests assume that the observations are statistically independent, which, in the case of adjacency matrices, they are not. To visualise this, consider that all the values along one row of an adjacency matrix pertain to a single node. If that node has a special quality, such as being very antisocial, it will affect all of their relations with others, introducing a lack of independence among all those cells in the row.

Another typical assumption of standard tests is that the variables are drawn from <u>a population with a particular distribution, such as a normal distribution. However,</u> many network population distributions are not normal.





Testing Hypotheses in Network Analysis

The main solutions to solve the problem of statistical testing of network hypotheses are two.

Using (and development) of statistical models specifically designed for studying the distribution of ties in a network (e.g., exponential random graph models and actor-oriented longitudinal models).

Using of a generic methodology of randomisation/permutation tests with (modified) standard methods, like regression. These methods are easy to use and interpret, and can be customised for different research questions — this is the path followed by UCINET.



Suppose we believe that a teacher favours tall kids. Hence, we hypothesise that height and exam scores in this teacher's classes are (positively) correlated.

To test our hypothesis, we let the teacher give all the students a test, measure their height, and then correlate the two variables. Let us say we get a moderate (Pearson's) correlation coefficient of 0.384. Is that number significant to asses our hypothesis or have we been just lucky and obtained a rare random configuration?

To remove the uncertainty, we might let the teacher give and grade a statisticallyrelevant number of tests (e.g., 100) and then perform our assessment with much more certainty.







Unfortunately, that procedure takes time.

E.g., if the teacher had three different classes (a reasonable amount of classes to teach to) and tested the students once per month (a reasonable amount of time for them to learn some new concepts to test), our study would take ~3 years (on a 10months/year schedule).

Still, we have concerns due to path dependence (knowledge debt of students) and we need to wait a lot of time for the study to be finished.

Is there a cheaper (time-, resource-wise) solution?

Let us make a thought experiment!







Instead of giving them tests, we let the students draw blindly (i.e., randomly) their scores from a box.

Then we ask "could it happen that most of the high scores happened to go to the tall people?" Unlikely, but it can happen indeed, we are trying to understand if that 0.384 correlation was random or not.

the blind-drawing experiment and compute how many times we get that 0.384 correlation value (and above).

avoiding path-dependency issues).



- How much unlikely? We can calculate the likelihood by just repeating e.g., 100 times
- Our randomised procedure helped us resolve a 3-year study in a couple of days (also









To find our solution, we essentially reversed the problem.

Instead of looking for certainty of correlation (the ~3-year study), we looked for certainty of non-randomness of the correlation.

(e.g., 20%) we cannot reasonably conclude that the teacher is biased.



E.g., if the percentile of cases in which we find those correlation coefficients is high



In permutation tests computers simulate millions of blind-drawings quickly and give us enough data to sufficiently test our hypotheses (of non-randomness).

A permutation test essentially calculates many (if not all) the ways that the experiment could have come out, given that scores were actually independent of height, and **counts the proportion** of random assignments yielding a correlation as large as the one actually observed.

That proportion is called the **p-value** or significance of the test and estimates the degree of confidence in rejecting the null hypothesis - usual measures are 5%, 1%, and 0,1%.





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Permutation Tests, a simple(r) example

E.g., we want to study whether lung diseases have a correlation with smoking.

Null hypothesis: there is no correlation between smoking and lung diseases, i.e., they are independent

Alt. hypothesis: there is a correlation between smoking and lung diseases **Alternative** Legend: Red, has disease. Square: smoker 0.6 **Observation:**

(Random) permutations:

-0.1 -0.1 0.6 0.6

Permutations that show the same ratio as the sample:



We cannot reject the null hypothesis (sample size problem).





Network Hypotheses

There are four main levels of analysis for network hypotheses:

- monadic hypotheses, e.g, "central people/nodes tend to be happier", are the closest to non-network ones and the correlation stands between a characteristic of the node (e.g., centrality) and another (e.g., happiness);
- dyadic hypotheses consider relations among pairs (dyads) of nodes, e.g., "the shorter the distance between two people's offices, the more they communicate over time", and are normally organised as $N \times N$ matrices we correlate;
- **mixed** hypotheses consider the relation between monadic and dyadic properties, e.g., "does the gender (monadic property) of a person affect whom that person is friends (dyadic) with?". Oftentimes these kinds of hypotheses are tested as dyadic by rephrasing the monadic property;
- network-level hypotheses consider the structure of the network with respect to some variable, e.g., "does the structure of the network determine the time a group finds a solution?", with the cases being whole networks instead of nodes.













Monadic Hypotheses

Regression testing do not make assumptions on the independence of variables and can be used to test monadic hypotheses of network data.

Regression coefficients.

The algorithm:

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- 1. performs a standard multiple regression across the corresponding cells of the vectors;
- regression, storing the resulting values;
- 3. Repeat 2. until it can properly estimate the standard errors for the statistics of yielded a coefficient as the one computed in 1.

	1	2	3	4	
	Coef	Beta	SE	Т	c.9
tercept #PRIORS	26.986 0.601	0.000 0.422	12.449 0.345	1.740	0.1

2. randomly permutes the elements of the dependent vector and recomputes the

interest. For each coefficient, we count the proportion of random permutations that





Dyadic Hypotheses

The Quadratic Assignment Procedure (QA technique designed to correlate whole ma is frequently used to test dyadic hypothes

Briefly, the technique tests the correlation matrices by reshaping them into thousand random-yet-similar pairs.

To do that it takes the data matrices and rearranges their rows (and matching colur Because this is done randomly, the result are independent from the data matrix the but they preserve the properties of the or mean, standard deviation, number of edg of cliques, etc).

To obtain the p-value, QAP counts the protect the random configurations that have a cocoefficient as large as the one observed.

Matrix: QAP Correlations

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Monadic-to-dyadic Hypotheses

The standard approach to testing the association between a node attribute and a dyadic relation is to convert the problem into a purely dyadic hypothesis by constructing a dyadic variable from the node attribute.

There are two main techniques to do this conversion, depending on whether the monadic attribute is scalar or nominal.

- B is 43, then the value of the "age" relation between them is 19.
- dyadic attributes by exact match, e.g., A and B are "clerks" while C is a neither A nor B.

- scalar attributes, e.g., age, wealth, height, can be converted into dyadic attributes as a comparison between the values of the two nodes. E.g., A is 24 years old and

- nominal attributes, e.g., role, gender, political affiliation, can be converted into "manager", then A and B have a relation (the match) while C has no relations with









Whole-network Hypotheses

We can use normal correlation tests where we can make the (statistics) classical assumption that the networks are obtained via a random sample.

If that assumption falls, we can resort to permutation tests and contrast the correlation coefficient between the groups/ networks and the dependent variable.

While permutation tests can help in assessing the significance of observations in a given (non-random) sample, the <u>results derived</u> from the latter <u>are not general as the one of the random</u> <u>one</u>.

The permutation results obtained from a nonrandom sample are significant for that sample, however, since we do not represent the whole population, as we lost generality—e.g., that teacher favours tall students, but we cannot extend that observation to other teachers.



